Neutrons



photons

The Complementarity of Real Space and Reciprocal Space

Lecture at Neutron and X-Ray School

J. Murray Gibson June 12, 2009



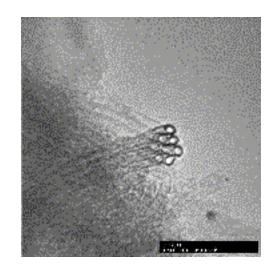
Outline

- Hour 1 theory
 - Imaging/diffraction and Fourier optics
 - electrons, x-rays and neutrons....
- Hour 2 examples
 - Picking the right tool for the problem

emphasize electron and x-ray microscopy as complementary tools

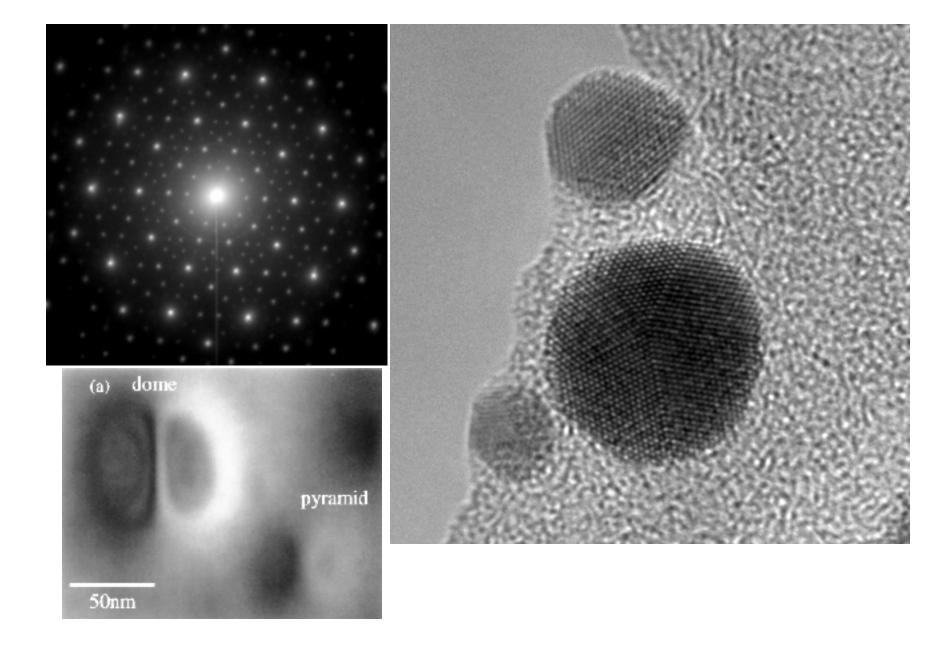
Why real-space?

- Yawn
 - I thought we were there already....
- Magnification
 - direct imaging of atoms..
- Diffraction Contrast
 - fourier optics



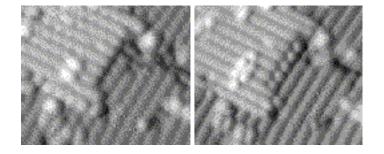
Smalley, Rice University

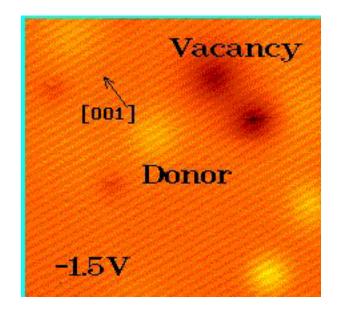
Microscopy with diffracting radiation



Scanning Probe Microscopy

Atoms moving on a silicon surface



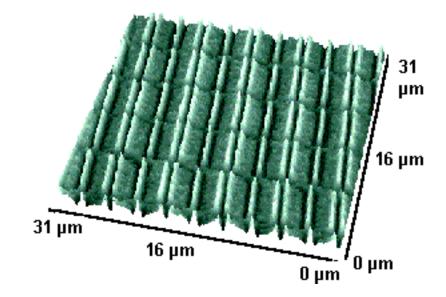


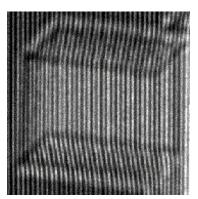
Imaging electronic states from dopants and imperfections in semiconductors

New Probes..

e.g. Magnetic Force Microscopy of a Hard Disk

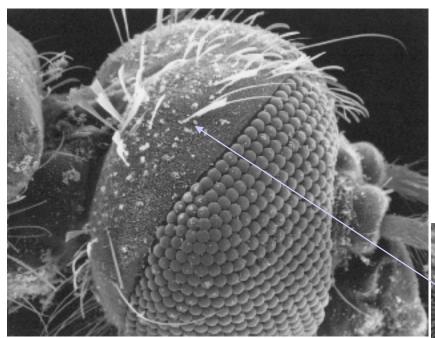






Related magnetic imaging - SEMPA, TEM Holography

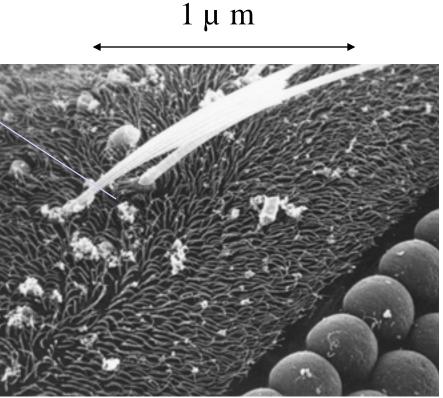
Mosquito head and compound eye



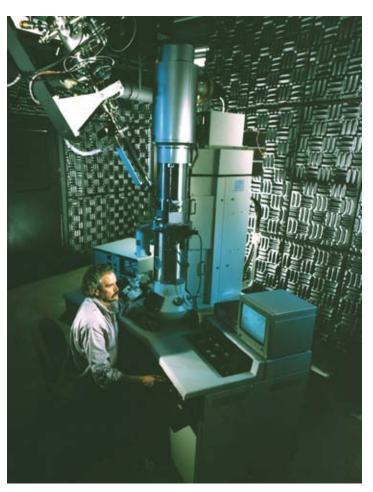
note depth of field

Scanning
Electron
Microscopy

Surface - "no" diffraction



US Electron Beam Microcharacterization Facilities

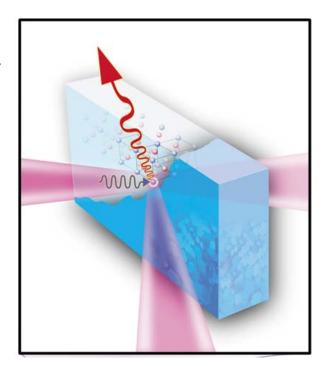


Argonne National Lab

- **4 DOE National Centers**
- -specialized techniques
- -new aberration correctionproject TEAM
 - 26 NSF MRSEC Centers
 - broad central facilities
 - ~100 other smaller centers
- typically single instrument

X-Ray Microscopy

- Hard x-rays focused to 30 nm ("Nanoprobe")
 - Nanoscale strain measurement
 - Imaging of domains, e.g., in ferroelectrics
 - Magnetism
 - Fluorescence spectro-microscopy
- Aiming at sub 10nm resolution
- Now operating jointly with the Center for Nanoscale Materials at ANL



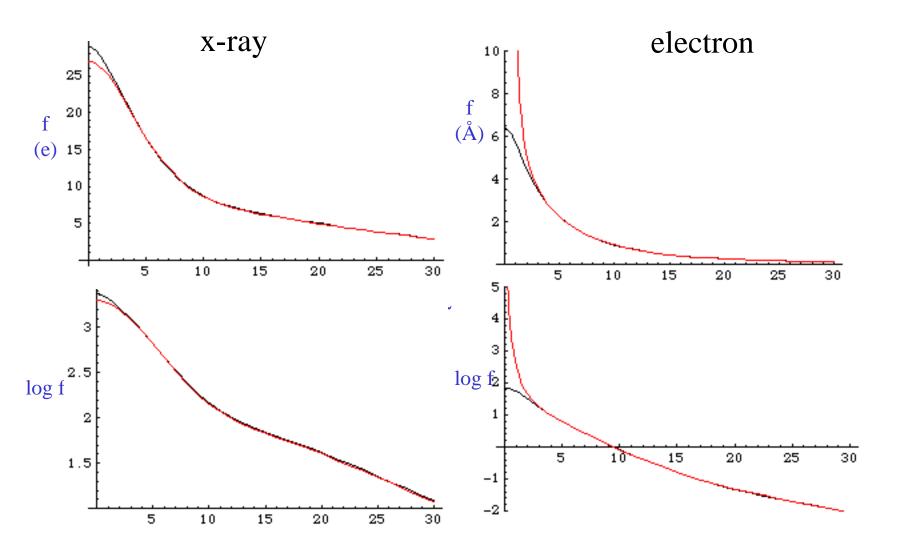
Electron Scattering

$$f_{X}(k) = \iint \rho(\underline{r})e^{i\underline{k}\bullet\underline{r}}d^{3}r \qquad f_{el}(k) = \iint V(\underline{r})e^{i\underline{k}\bullet\underline{r}}d^{3}r$$

$$\nabla^2 V(\underline{r}) = -\frac{\rho(\underline{r})}{\mathcal{E}_0}$$

$$f_{el}(k) = a \frac{(Z - f_x)}{k^2}$$
 Mott Formula

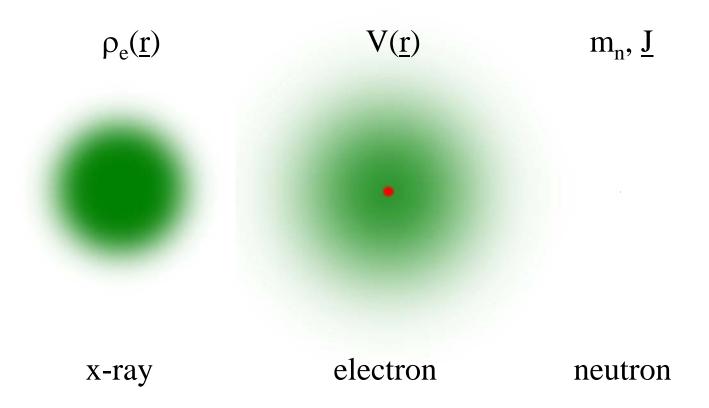
Atom Form Factors



Sensitivity of form factors to charge

d spacing (Å)	change in f x (%)	change in f el (%)		
2	-0.7	2.1		
4	-3.4	32.3		
8	-5.7	199.0		

What the particle sees....



Electron Form Factors

- Similar dependence on Z
- At high angles Rutherford-like

$$f_{el}(k) = a \frac{Z}{k^2}$$

Advantages/Disadvantages

Thermal Neutrons

λ~d_{hkl}
penetrates
strong contrast possible (e.g. H/D)
E~elementary excitations
strong magnetic scattering

Synchrotron X-rays

 $\lambda \sim d_{hkl}$ high brilliance no kinematic restrictions no ΔE restriction

low brilliance some elements absorb strongly restrictions on Q for large ΔE excitations < 100meV

strong absorption at low E little contrast e.g. H-C weak scattering from light elements radiation damage

Fast Electrons

 $\lambda << d_{hkl}$ high brilliance, nanoprobes no kinematic restrictions no ΔE or ΔQ restriction charge sensitive

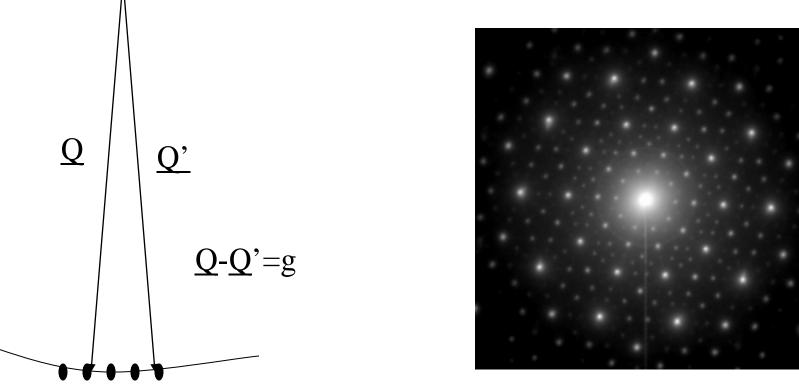
thin samples (or surfaces) dynamical scattering little contrast e.g. hydrocarbons weak scattering from light elements radiation damage

courtesy Sunil Sinha

Complementarity of techniques

Radiation	Source Brightness (particles/cm²/ steradian/eV)	Elæstic Mean- Free Path (Å)		Minimum Probe Size (Å)
Neutrons	10 ¹⁴	10 ⁸	10 ⁹	10 ⁷
X-rays	10 ²⁶	10 ⁴	10 ⁶	10 ³
Electrons	10 ²⁹	10 ²	10³	1

Electron Diffraction



Ewald sphere "flat"

Kinematic theory c.f. x-rays/neutrons predicts diffraction pattern geometry, qualitative effects

Dynamical Theory of Diffraction

$$\frac{d\phi_0}{dz} = \frac{i\pi}{\xi_0}\phi_0 + \frac{i\pi}{\xi_g}\phi_g e^{2\pi isz}$$

$$\frac{d\phi_g}{dz} = \frac{i\pi}{\xi_g} \phi_0 e^{-2\pi i s z} + \frac{i\pi}{\xi_0} \phi_g$$

2-beam theory can be extended to N beams

- BLOCH WAVES

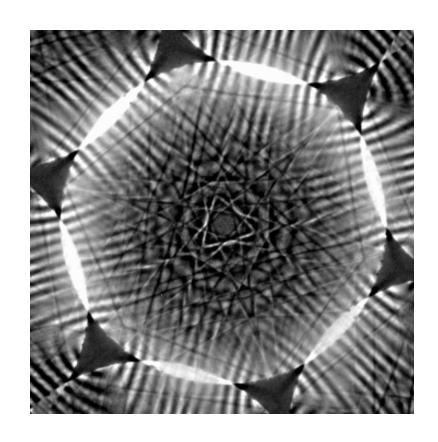
Extinction distance:

$$\zeta_g = \frac{\pi\Omega}{\lambda F}$$

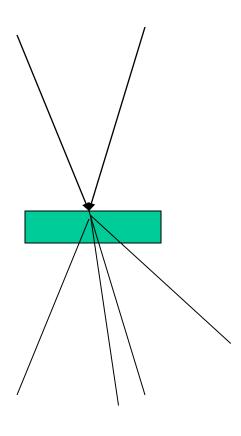
typically ~1000 Å at 100kV

absorption is added as an imaginary extinction

Convergent Beam Electron Diffraction



Si (111)



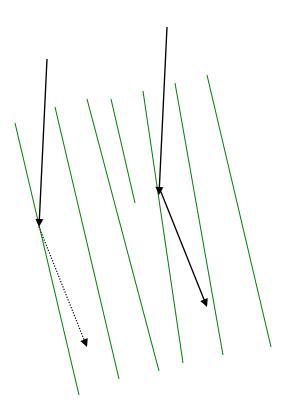
reveals full symmetry

Imaging

The column approximation:

$$\frac{d\phi_0}{dz} = \frac{i\pi}{\xi_0} \phi_0 + \frac{i\pi}{\xi_g} \phi_g e^{2\pi i(sz + g \cdot dR/dz)}$$

$$\frac{d\phi_g}{dz} = \frac{i\pi}{\xi_g} \phi_0 e^{-2\pi i s z} + \frac{i\pi}{\xi_0} \phi_g$$



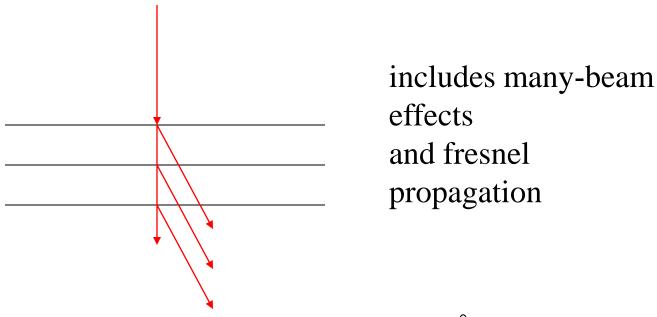
edge dislocation displacement field \underline{R}

Howie-Whelan Equations

predicts strain-contrast images well at ~20Å resolution

Multi-slice theory

More accurate but less-efficient approximation propagates electrons between thin (kinematical) slices



appropriate for high-resolution (<5Å) imaging

Fourier Optics

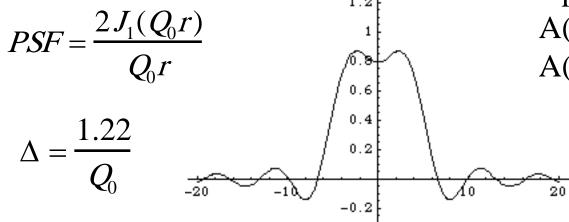
- Diffraction and Imaging
 - Fraunhofer diffraction $F(\underline{Q}) = \iint \phi(\underline{r}) e^{i\underline{Q} \cdot \underline{r}}$
 - one fourier transform
 - Imaging (with a lens) $\varphi(\underline{r}) = \iint F(\underline{Q})e^{-i\underline{Q} \cdot \underline{r}}$
 - Second fourier transform
 - It gets interesting when you filter in one space or the other

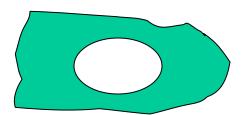
Simple Consequence

• Abbe's theory of the microscope resolution

$$\varphi(\underline{r}) = \iint A(\underline{Q}) F(\underline{Q}) e^{-i\underline{Q} \cdot \underline{r}}$$

- =convolution with F.T. (A)
- and the Rayleigh Criterion

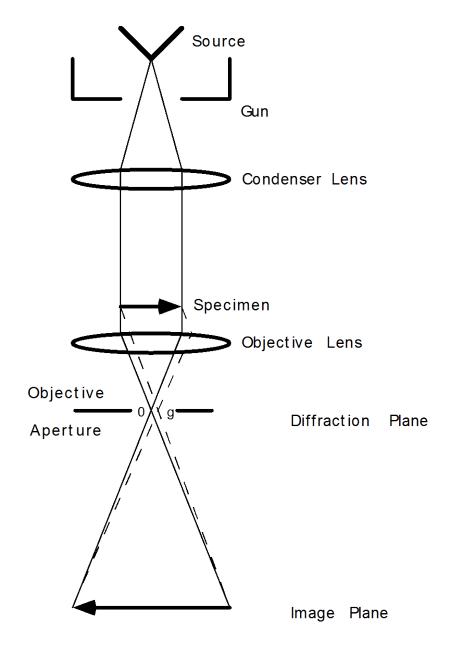




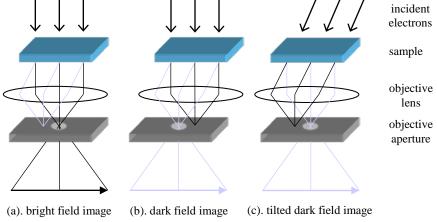
Aperture in focal plane

$$A(Q) = 1; Q < Q_0$$

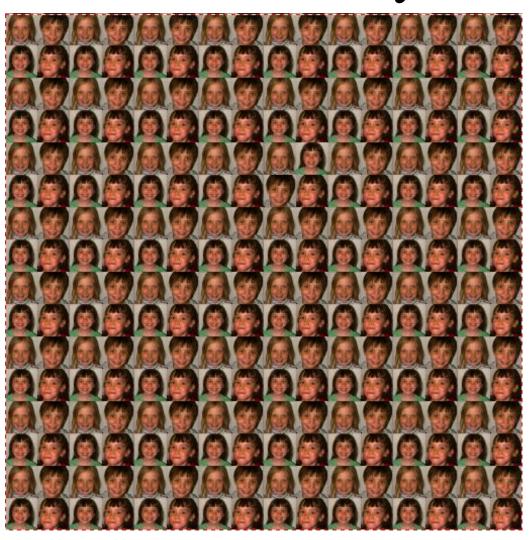
$$A(Q) = 0; Q > Q_0$$



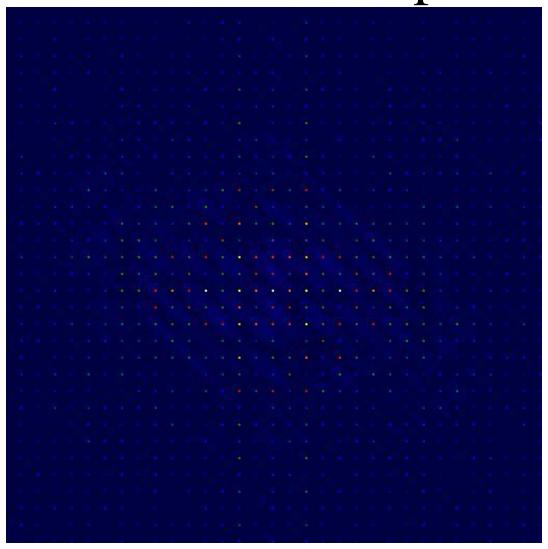
Bright and Dark Field Imaging



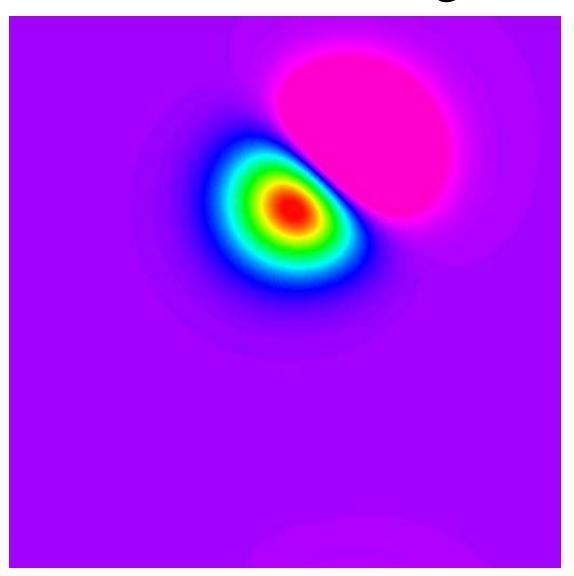
A 2-D Perfect Crystal?



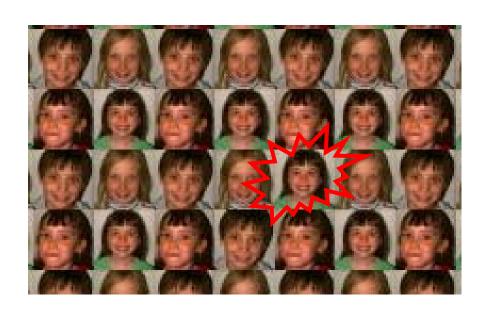
and it's diffraction pattern



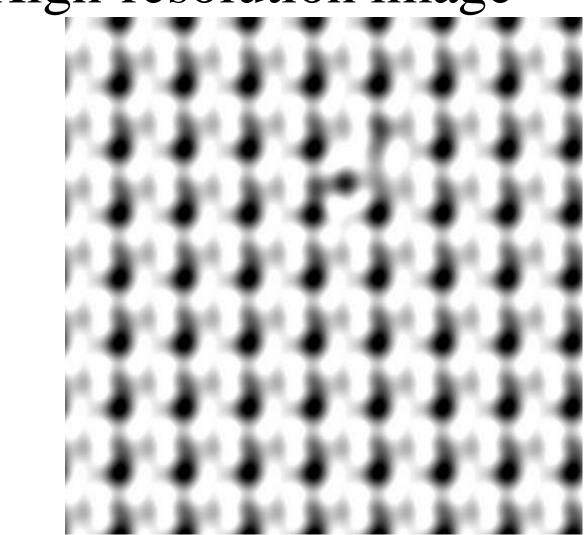
Dark-field image



The point defect...

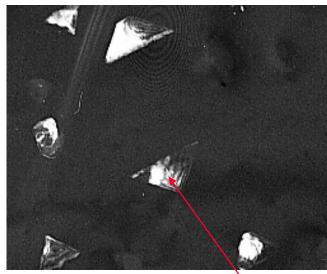


"High-resolution image"

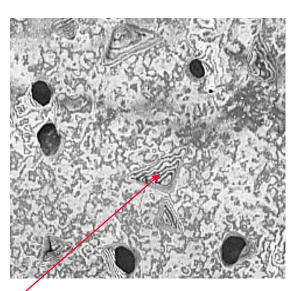


Amplitude Contrast Imaging

Cu₂O Reflection

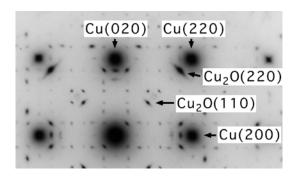


Cu Reflection



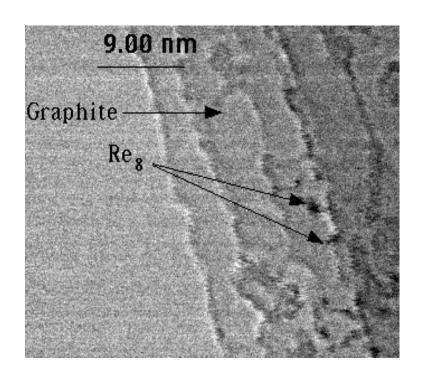
Mixed phase system..

Self-limiting oxidation of copper Yang, JC; Kolasa, B; Gibson, JM, APPLIED PHYSICS LETTS, 73, 2841 (1998) same island



Scanning Transmission Electron Microscopy

"Z-Contrast" STEM



Re 6

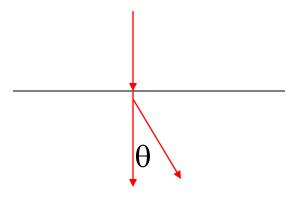
Bright-field STEM Image

High-angle ADF dark-field image

The principle of reciprocity..

Phase Contrast and High Resolution

- To image lattice resolution < d
 - $\Rightarrow Q_0 > g$ so no amplitude contrast



fresnel phase shift $\sim \pi/\lambda z\theta^2$

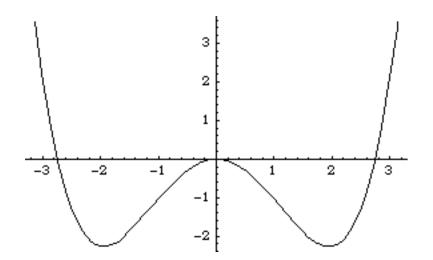
assume object is weak phase shift (kinematical theory)

$$\psi = e^{i\sigma V(\underline{r})} \approx 1 + i\sigma V(\underline{r})$$

You want a phase shift near $-\pi/2$ (Zernicke phase contrast)

Phase shift with aberrations

Phase shifting function (should be near $-\pi/2$)



$$\gamma = \pi \lambda (zk^2 + C_s k^4 / 2)$$
$$k = \frac{q}{2\pi}$$

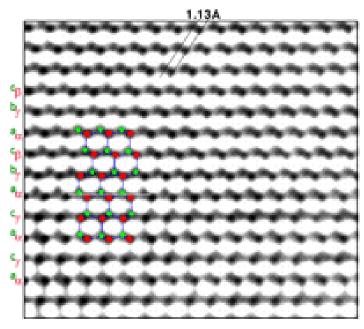
C_s is the spherical aberration coefficient

Ideal defocus (Scherzer) $z = -1.2\sqrt{C_s\lambda}$ $\Rightarrow r = 0.67(C_s\lambda^3)^{1/4}$ point-to-point resolution

State of the art high-resolution

GaN (LBL)

this picture shows reconstructed electron wavefunction revealing split Ga/N atoms

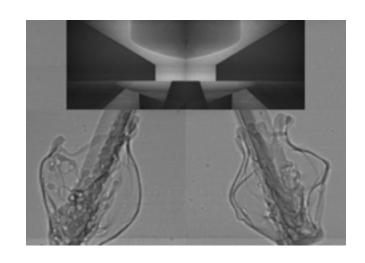


removing the microscope aberrations - wavefront reconstruction, aberration correction

Phase Contrast X-Ray Imaging



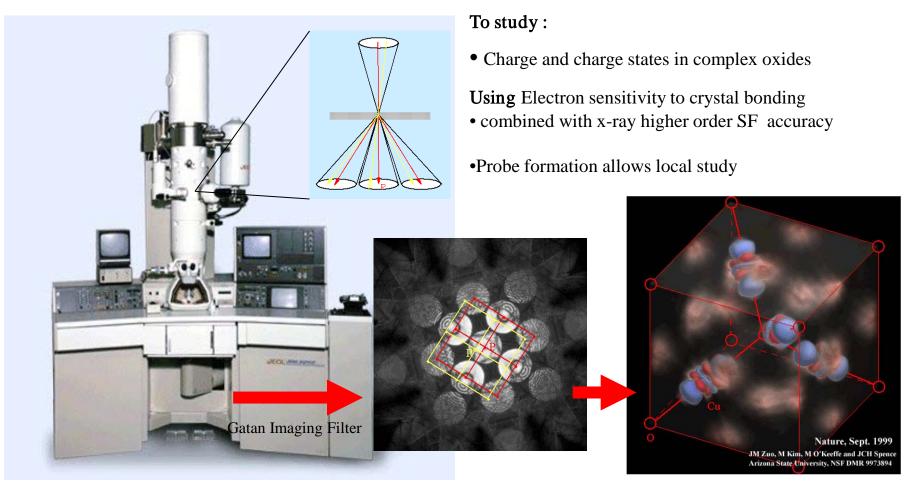
Big bugs, Socha et al., PNAS **104**, 13198, (2007)



Fuel Sprays: Wang, YJ et al. NATURE PHYSICS, 4 305 (2008)

Examples

Quantitative determination of local structure and charge distribution in copper oxide

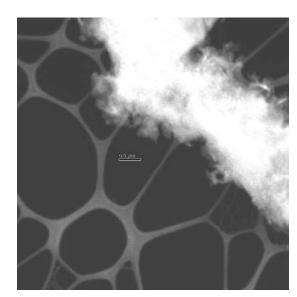


Crystallites in glass

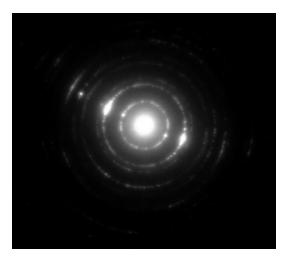
- Recent experience with IPNS experiment
- Thermal poling of SiO₂ induced optical nonlinearity
 - Initial IPNS data suggested structural change in amorphous
 material (Cabrillo, Gibson, Johnson, Bermejo et. al.)
- TEM shows ~5% small crystallites (critobalite)

unpoled





poled



Role of microscopy in confirming homogeneity

Self-limiting oxidation of copper

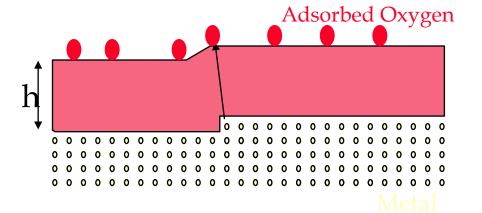
J. C. Yang, a) B. Kolasa, and J. M. Gibson

Materials Research Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801

M. Yeadon

Institute of Materials Research and Engineering, National University of Singapore, 119260, Singapore

assumes cation drift in uniform film $1/h = A - B \ln(t)$



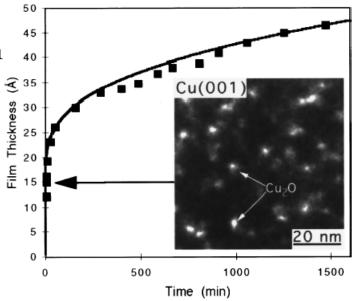
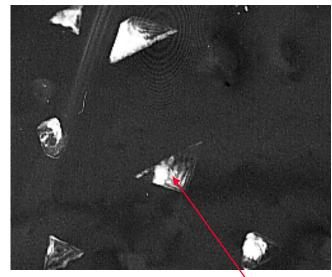


FIG. 1. Oxide thickness Cu_2O of vs time from Young et al. (see Ref. 2) of the thickness of the Cu_2O as function of time, when single crystal (001) Cu was oxidized in 760 Torr O_2 at 70 °C. The arrow points to the experimental condition we used. (Inset) Dark field image from the Cu_2O reflection, where the bright specks are Cu_2O islands.

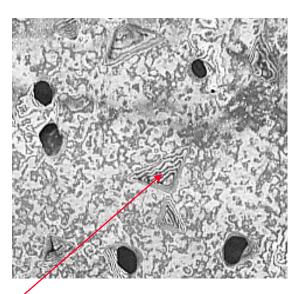
N.Cabrera, N.F. Mott, Rept. Progr. Phys. 12, 163 (1948)

Dark-field imaging of phases

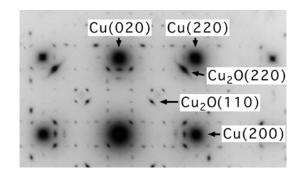
Cu₂O Reflection



Cu Reflection

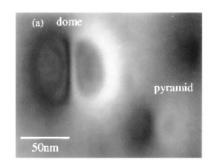


same island



Strain Evolution in Coherent Ge/Si Islands

Chuan-Pu Liu,1,* J. Murray Gibson,1 David G. Cahill,1 Theodore I. Kamins,2 David P. Basile,2 and R. Stanley Williams2



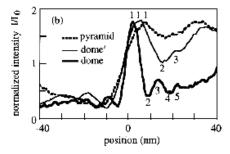


FIG. 1. Dark-field images of a pyramid and a dome using $\mathbf{g} = 400$. (b) Line traces across three typical islands found in the experiment, where the fringes on one side of the images are numbered.

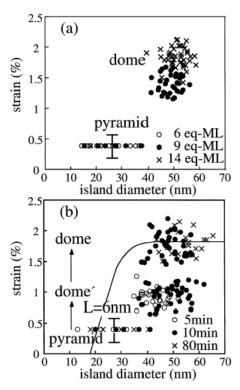
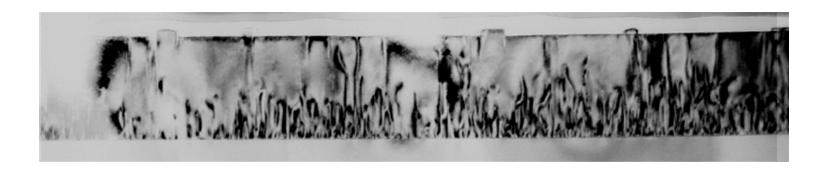


FIG. 2. Strain in Ge islands vs island diameter. (a) For asdeposited samples 6, 9, and 14 eq-ML thick grown at 600 °C and (b) for 8 eq-ML thick samples deposited at 550 °C and annealed at 550 °C for 5, 10, and 80 min. The error ranges both in diameter and strain are 10%. The solid curve in (b) represents the dependence of the island diameter on the strain of equilibrium islands with isotropic surface energies, derived from the work of Kukta and Freund [17] using L=6 nm (see text for details). The island populations in a sample annealed for 40 min are similar to that for 80 min (data not shown).

Defect Imaging



Threading dislocations in GaN

Strain contrast imaging of defects

- allows determination of burger's vector

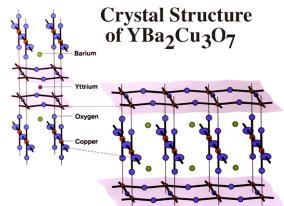
Density (/cm ²)
Technique

10 ¹⁴

10¹² TEM 10 ⁴

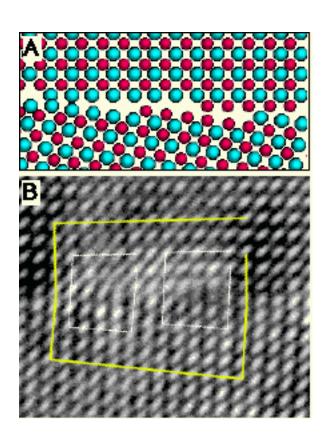
High T_c Superconductors

- Neutron Diffraction -
 - crystal structure
- X-Ray Photoemission
 - understand pairing mechanism?
- Transmission Electron Microscopy
 - Thin film structure and defects
 - Grain Boundaries
 - Understand J_c





Interface Science

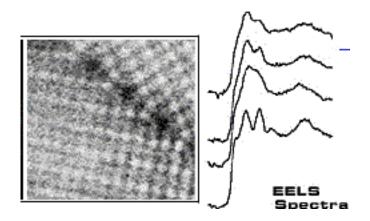


Atomic structure of grain boundary in zirconia

Merkle ANL

http://www.msd.anl.gov:50610/groups/im/highlights/yszmicroscopy/ysz.html

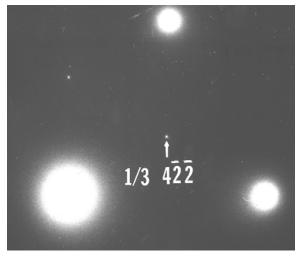
"Atomic Scale" Spectroscopy



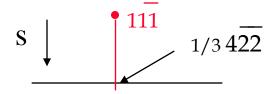
Browning, U. Illinois Chicago

near-edge structure of oxygen near a zirconia boundary

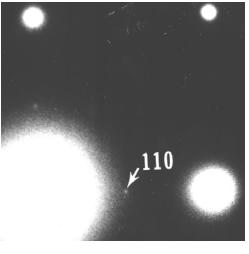
Surface/Interface Roughness



Silicon (111)



zero-order laue-zone

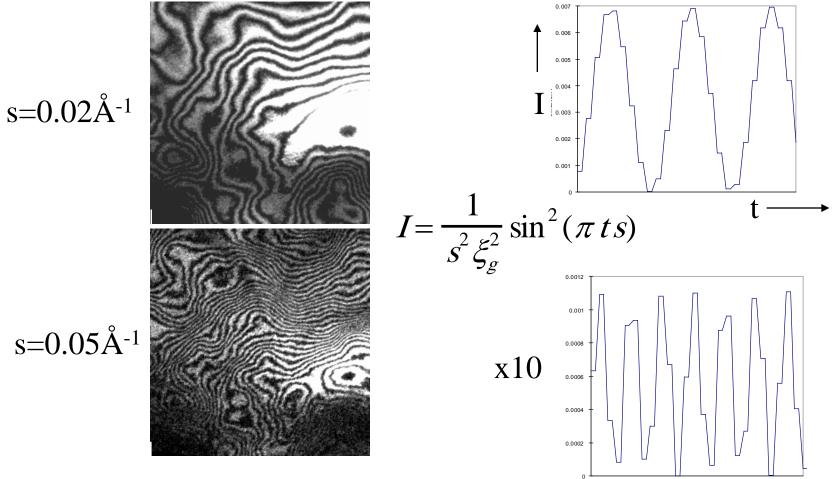


Silicon (100)

Crystal Truncation Rods

Chen and Gibson, Phys. Rev. B **54**, 2846 (1996)

Imaging Roughness

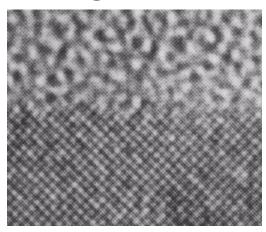


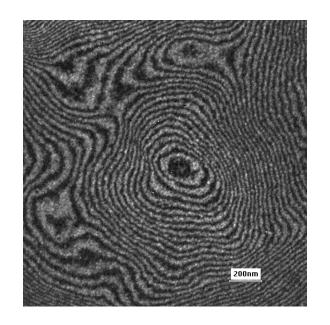
"diffraction contrast" dark field imaging

Transmission Electron Microscopy and Roughness

• familiar in cross-section

but limited by projection, and sampling

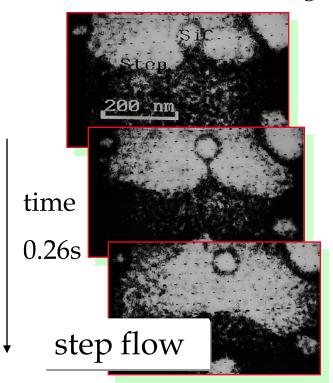




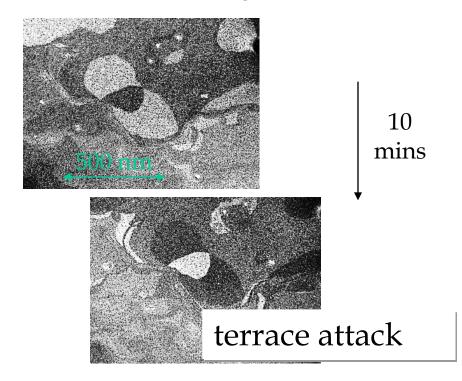
Our method uses plan-view imaging limited to specially prepared samples

Earlier work on dynamics of UHV oxidation/etching

SiO formation = etching



 SiO_2 formation = oxide growth



Ross, Gibson and Twesten, Surf. Sci. 310, 243 (1994)

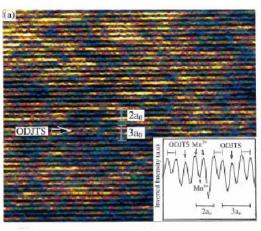
Diffuse scattering

Volume 81, Number 18

PHYSICAL REVIEW LETTERS

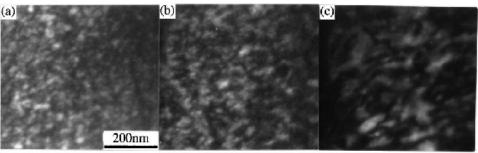
2 November 1998

Paired and Unpaired Charge Stripes in the Ferromagnetic Phase of La_{0.5}Ca_{0.5}MnO₃

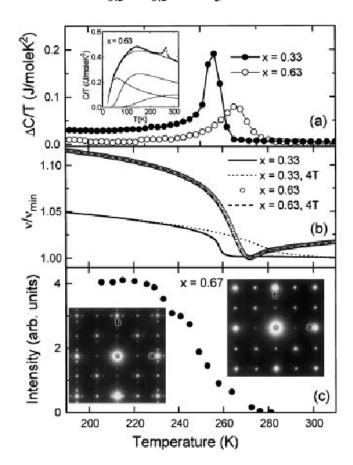


S. Mori, ^{1,*} C. H. Chen, ¹ and S-W. Ch Laboratories, Lucent Technologies, Murray Hil ¹Physics and Astronomy, Rutgers University, P (Received 9 April 1998)

existence of ferromagnetism and charge order nogenous spatial mixture of incommensurate crodomains with a size of 20-30 nm. Furthern te charge-ordered microdomains indicate a char d Jahn-Teller distorted Mn³⁺ stripes. We proper of the d_{z^2} orbitals. These results demonstrate separation. [S0031-9007(98)07522-X]



temp/ dep. domains (dark-field)



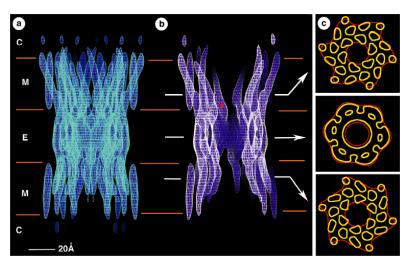
Structural Biology

Phasing reflections for large structures

Three-Dimensional Structure of a Recombinant Gap Junction Membrane Channel

Vinzenz M. Unger, 1* Nalin M. Kumar, 1 Norton B. Gilula, 1 Mark Yeager 1,2 †

Gap junction membrane channels mediate electrical and metabolic coupling between adjacent cells. The structure of a recombinant cardiac gap junction channel was determined by electron crystallography at resolutions of 7.5 angstroms in the membrane plane and 21 angstroms in the vertical direction. The dodecameric channel was formed by the end-to-end docking of two hexamers, each of which displayed 24 rods of density in the membrane interior, which is consistent with an α -helical conformation for the four transmembrane domains of each connexin subunit. The transmembrane α -helical rods contrasted with the double-layered appearance of the extracellular domains. Although not indicative for a particular type of secondary structure, the protein density that formed the extracellular vestibule provided a tight seal to exclude the exchange of substances with the extracellular milieu.

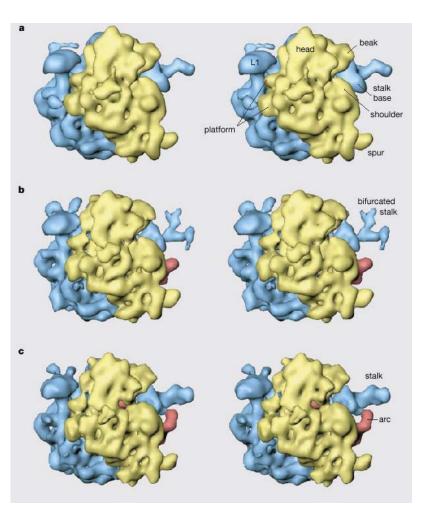


A ratchet-like inter-subunit reorganization of the ribosome during translocation

Joachim Frank*†‡ & Rajendra Kumar Agrawal†‡

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The ribosome is a macromolecular assembly that is responsible for protein biosynthesis following genetic instructions in all organisms. It is composed of two unequal subunits: the smaller subunit binds messenger RNA and the anticodon end of transfer RNAs, and helps to decode the mRNA; and the larger subunit interacts with the amino-acid-carrying end of tRNAs and catalyses the formation of the peptide bonds. After peptide-bond formation, elongation factor G (EF-G) binds to the ribosome, triggering the translocation of peptidyl-tRNA from its aminoacyl site to the peptidyl site, and movement of mRNA by one codon¹. Here we analyse three-dimensional cryo-electron microscopy maps of the *Escherichia coli* 70S ribosome in various functional states, and show that both EF-G binding and subsequent GTP



x-ray structure this year depended on 7.5 Å e-structure

Nanoscience

Nanomechanics of Individual Carbon Nanotubes from Pyrolytically Grown Arrays

Ruiping Gao, ^{1,4} Zhong L. Wang, ^{1,*} Zhigang Bai, ¹ Walter A. de Heer, ² Liming Dai, ³ and Mei Gao ³ ¹ School of Materials Science and Engineering, Georgia Institute of Technology, Atlanta, Georgia 30332-0245

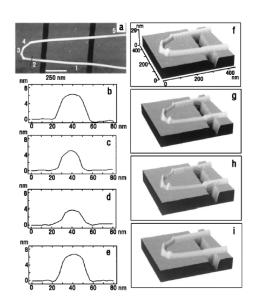


FIG. 1. Deformability of a MWCNT deposited on a patterned silicon wafer as visualized with tapping-mode AFM operated far below mechanical resonance of a cantilever at different set points. The height in this and all subsequent images was coded in gray scale, with darker tones corresponding to lower features.

AFM - Yu et. al. PRL 85, 1456, (2000)

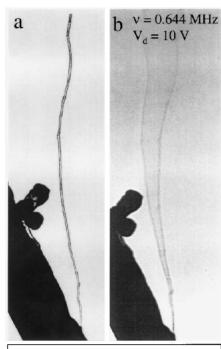
shear modulus

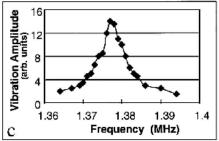
$$\nu_i = \frac{\beta_i^2}{8\pi} \frac{1}{L^2} \sqrt{\frac{(D^2 + D_1^2)E_b}{\rho}},$$

E~30 GPa

without defects
E~3 GPa

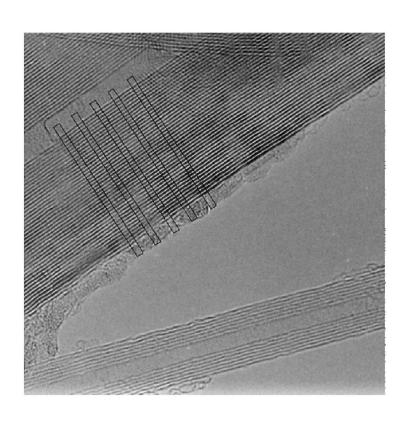
with defects

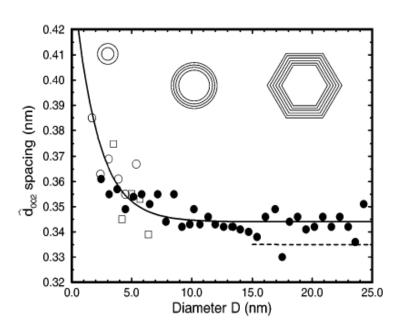




Size Effects in Carbon Nanotubes

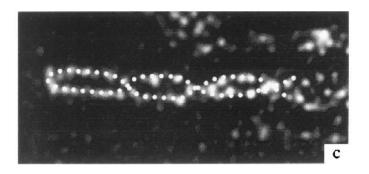
C.-H. Kiang, M. Endo, P. M. Ajayan, G. Dresselhaus, and M. S. Dresselhaus



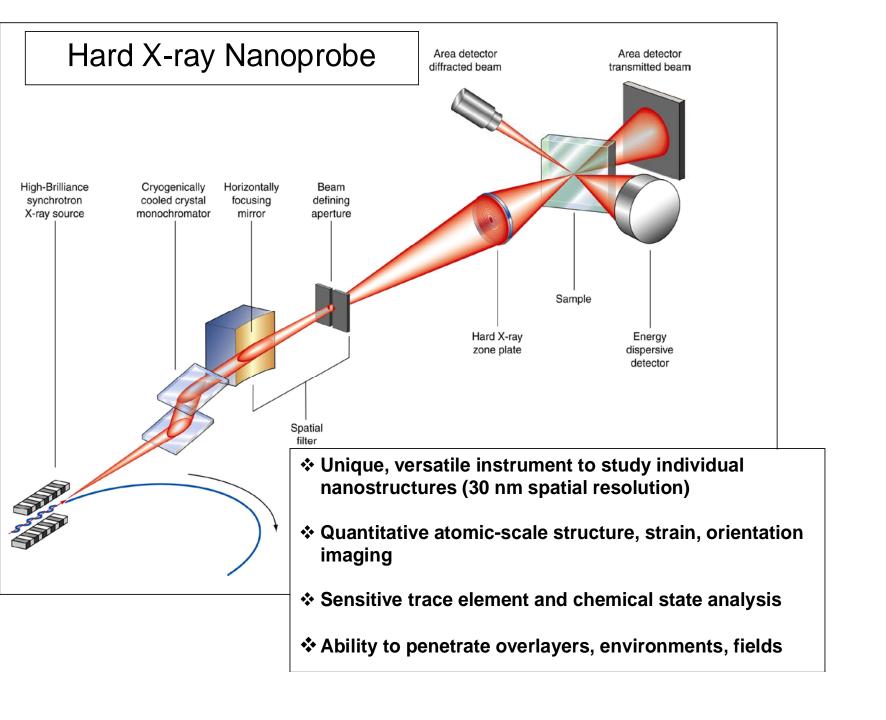


helicity plays a role in properties/structure

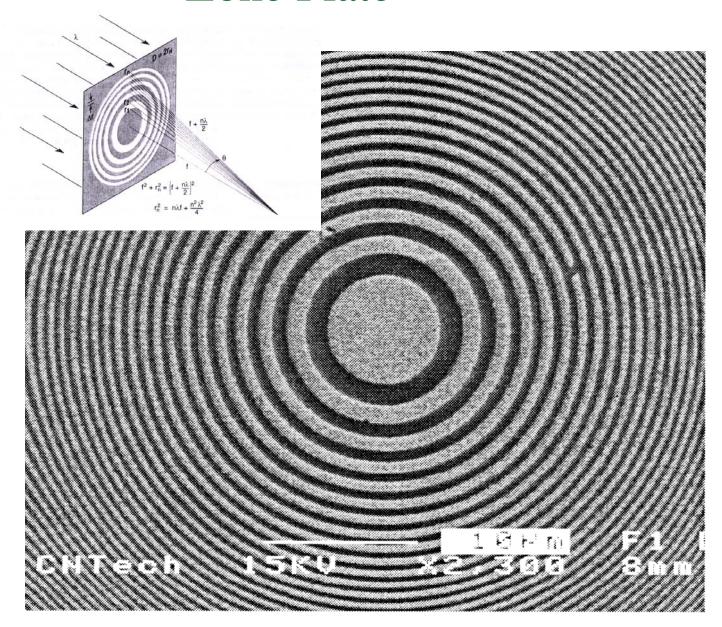
Applications of Z Contrast



Iodine atoms in 1nm diameter C-SWNT Fan. et al. PRL 84, 4621 (2000)

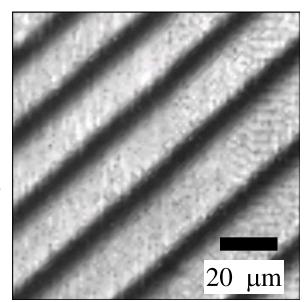


Zone Plate

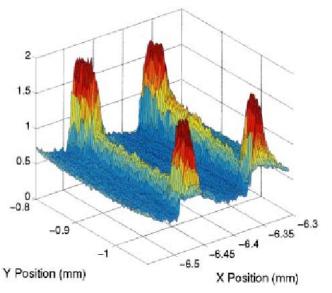


X-ray Microprobe Experiments

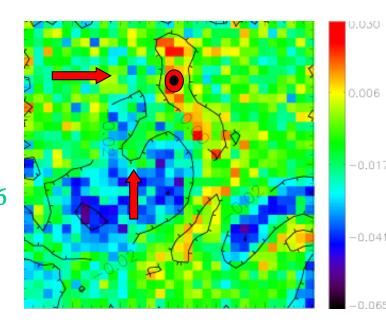
Nanometer-scale physics in ferroelectrics (P. Evans, Lucent)



Magnetization in HoFe₂
J. Pollmann, *et al.*, Rev. Sci. Instrum. **71** 2386 (2000).



Stress under metallization on Si (100) P.-C. Wang, et al., Appl. Phys. Lett. **76** 3726 (2000).

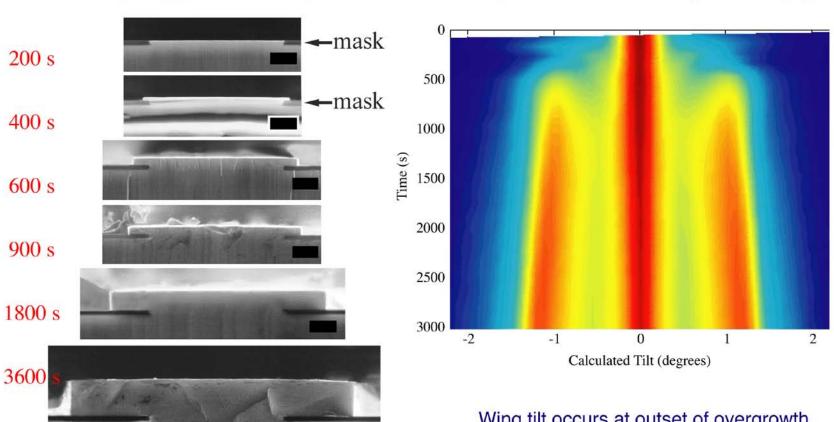


Real-Time X-ray Characterization of Patterned Growth

P. Fini et al., APL 76, 3893 (2000)

Growth morphology (ex-situ SEM):

In-situ X-ray measurement of wing tilt during growth:

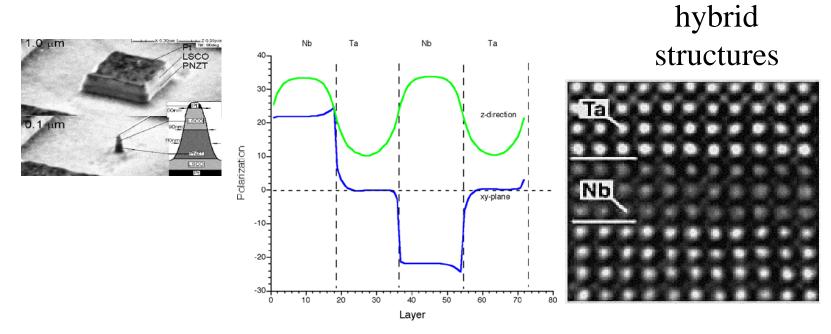


1 µm

Wing tilt occurs at outset of overgrowth, not during cooling

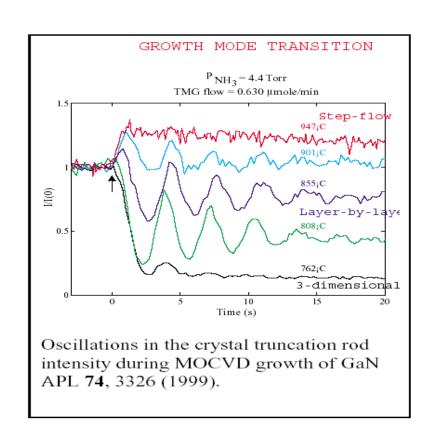
Nanoprobe diffraction studies of Nanopatterning - ETCHING

- Microfocused beam will allow illumination of individual nanostructures.
- Need to understand subtractive processes as well as additive (growth)
- Novel materials will be investigated (e.g., multicomponent oxides).



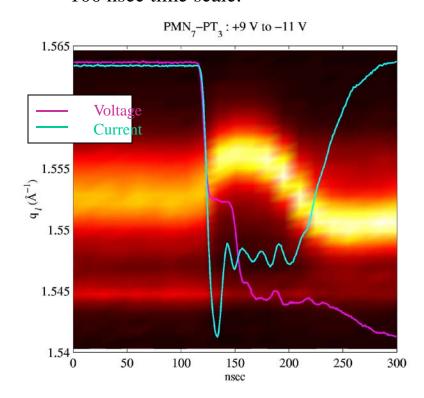
H. M. Christen et al., APL, <u>72</u> 2535 (1998)

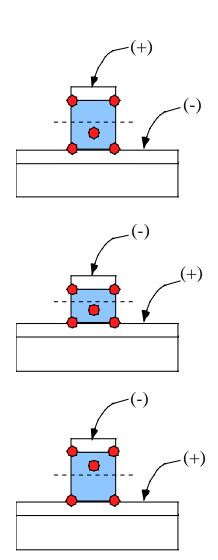
Studies of Growth and Etching



Time-Resolved Studies of Ferroelectric Switching

- Lattice parameter during switching has been measured with 17 nsec time resolution.
- Two-step response to voltage: prompt piezoresponse followed by switching on ~ 100 nsec time scale.



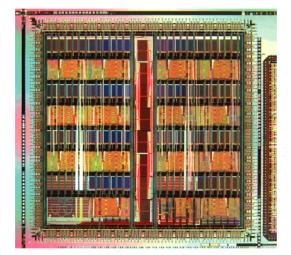


C. Thompson (NIU), S. Streiffer (ANL-MSD), A. McPherson (ANL-XFD)

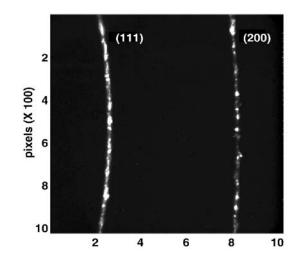
Measurement of Strain in Al-Cu Interconnect Lines

Using X-ray Microdiffraction

- Reliability of integrated circuit Al-Cu interconnects in electronics impacted by electromigration and mechanical stress.
- X-ray microdiffraction from interconnects reveals origin and details of microscopic stress.
- Can lead to increasingly reliable devices (computers, etc.) even as they become more complex.

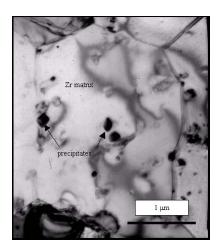


Fast Fourier transform integrated circuit (Special Purpose Processor Development Group, Mayo Clinic)



Microdiffraction pattern from a thick-blanket Al-Cu film.

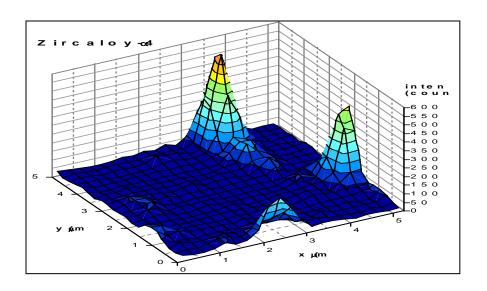
X-Ray Fluorescence Microscopy complementary to Transmission Electron Microscopy



Transmission
Electron
Microscopy of
Zircalloy grain

	Zircaloy-4	ZIRLO
	(weight %)	(weight %)
Fe	0.24	0.11
Cr	0.11	0.001
Sn	1.64	1.08
Ni	0.0034	<0.001
Nb	-	1.23
0	0.112	0.145
Cu	0.002	0.002
Hf	<0.004	<0.004

Measured overall compositions



Examining compositions in metal alloy precipitates

X-Ray fluorescence imaging of single bacterial cells

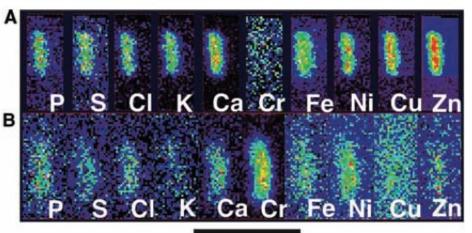
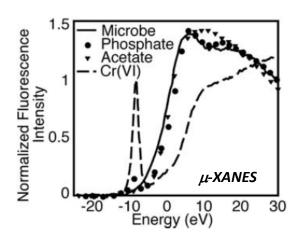


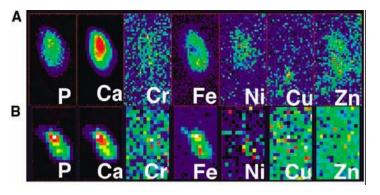
Fig. 1. False-color micro-XRF maps of qualitative spatial distributions and concentration gradients of elements in and around planktonic *P. fluorescens* microbes harvested before (A) and after (B) exposure to potassium dichromate [Cr(VI)] solution (1000 ppm) for 6 hours.

Kemner et al. Science 306, 686 (2004).





→ Redox states Cr(III)



A: planktonic bacterium cell before exposure to Cr

B: planktonic cell after exposure to 1000 ppm Cr(VI)

Isolated planktonic cell accumulates Cr, looses 'typical' cellular elements, and stains 'dead'

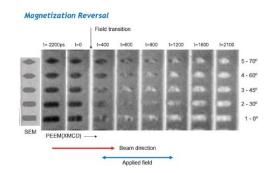
Surface adhered cell does not take up Cr, shows no change in elemental content, and remains alive

Attachment of prokaryotic cells to surfaces modulates elemental content and response to environmental challenges

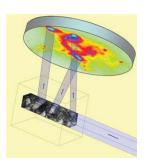
Advanced X-ray imaging reveals hierarchical structure



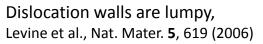
The effect of different exercise regimens on bone – S. Stock, NWU 2-BM



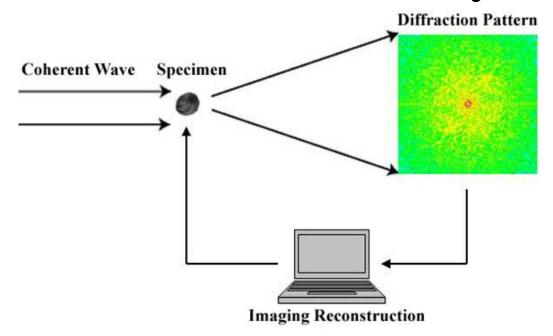
Magnetic instability regions in patterned structures Han et al., Phys. Rev. Lett. **98**, 147202 (2007)



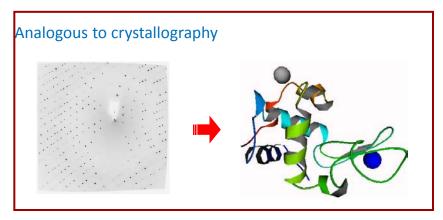
Big bugs, Socha et al., PNAS **104**, 13198, (2007)

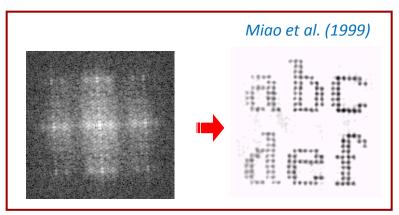


Coherent X-Ray Diffraction

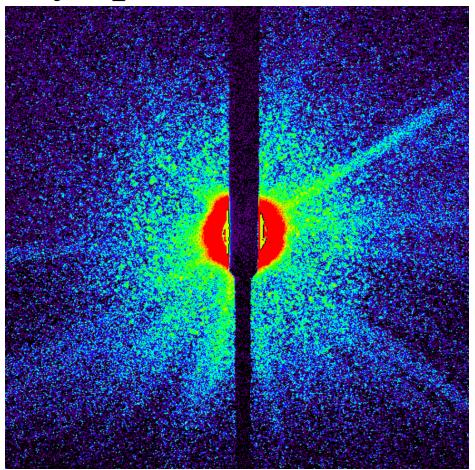


- → Coherent diffraction imaging is much like crystallography but applied to noncrystalline materials
- → First proposed by David Sayre in 1980, and first experimental demonstration by John Miao et al in 1999 using soft x-rays
- → Requires a fully coherent x-ray beam





Soft x-ray speckle of static aerogels

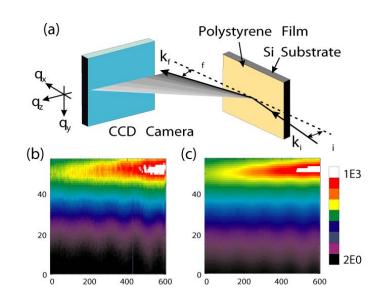


Speckle pattern produced by aerogel sample (0.014 g/cm³). Pattern was recorded with 1.83 keV x-rays using a 5- μ m pinhole source and monochromatic (E/ Δ E ~ 1000) beam.

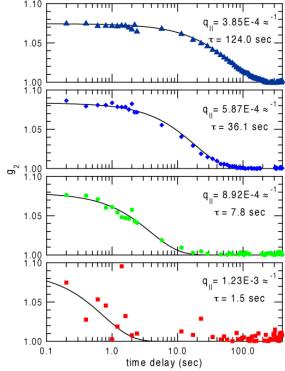
Ian McNulty, APS

Surface dynamics of polymer films

 Motivated by reports that T_g at the surface of polymer films is reduced Kim, Ruehm, Lurio, Basu, Lal, Mochrie, and Sinha used XPCS at 8-ID to characterize the relaxation of thermally excited height fluctuations on the surface of polystyrene(PS) films to investigate how the near-surface viscosity might differ from that of the bulk PS.



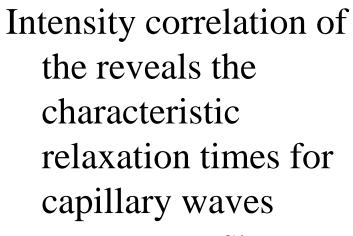
Surface Dynamics of Polymer



Films

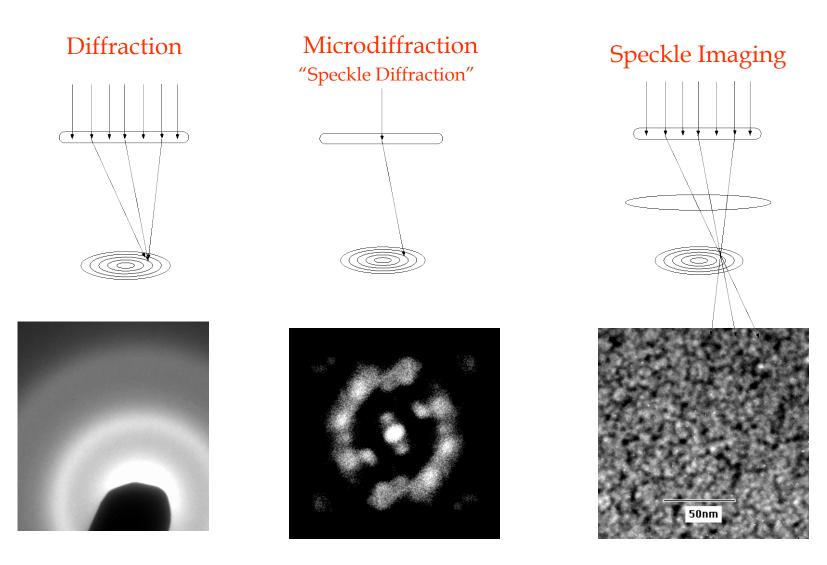
1E-3

1.0E+0



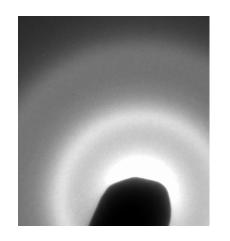
Shows no change in T_o near surface

Fluctuation (Electron) Microscopy



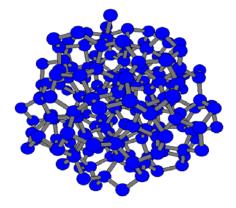
"coherent diffraction"

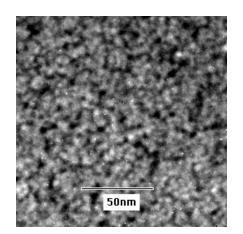
New structural information from glasses - Fluctuation Microscopy



Diffraction => Pair Correlation Function

=>short-range order

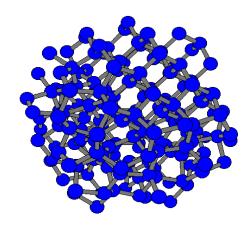




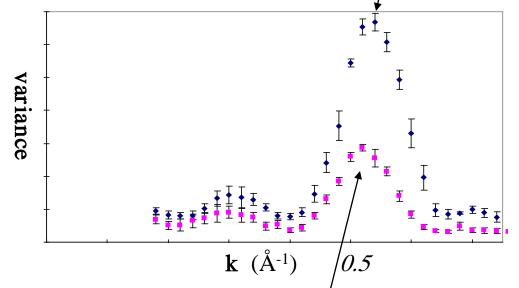
Imaging (speckle) =>Pair-Pair Correlation
Function

=>medium-range order

Paracrystallinity in a-Si/Ge



Important effects on thermodynamic and physical properties electrical stability, impurity diffusion Medium-range order (~15Å) found in deposited amorphous semiconductors / - not seen by diffraction



Become more like random hetworks on annealing or light soaking in a-Si(H)

Gibson et. al., Phys. Rev. Lett. **78**, 1074 (1997); Appl. Phys. Lett **73**, 3093 (1998).

Further Reading

- "Electron Microscopy of Thin Crystals", Hirsch et. al. (Kreiger, New York 1977)
- "Diffraction Physics", J.M. Cowley, (North Holland, Amsterdam 1981)
- "Transmission Electron Microscopy", L. Reimer, (Springer-Verlag, Berlin 1984)
- "Transmission Electron Microscopy: A Textbook for Materials Science", D.B. Williams and C.B. Carter, (Plenum, New York 1996)